



# The effect of structural evolution on the magnetocaloric properties of Cu-added GdHoErNi high-entropy alloys

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## ABSTRACT

The  $(\text{Gd}_{25}\text{Ho}_{25}\text{Er}_{25}\text{Ni}_{25})_{100-x}\text{Cu}_x$  ( $x = 0, 10$ , and  $20$ ) high-entropy alloys (HEAs) were obtained after compositional design and melt-spinning technology. The Curie temperatures of the  $(\text{Gd}_{25}\text{Ho}_{25}\text{Er}_{25}\text{Ni}_{25})_{100-x}\text{Cu}_x$  ( $x = 0, 10$ , and  $20$ ) alloys are  $41$ ,  $45$ , and  $42$  K, respectively, lying in the temperature range required by hydrogen liquefaction, i.e.,  $20$ – $77$  K. The Cu-free alloy shows an amorphous/nanocrystalline dual-phase structure with an enrichment of Ni element within the minor amorphous phase. The Cu-added alloys exhibit a fully amorphous structure with a uniform distribution of elements. The structure evolution of the studied alloys is attributed to the enhanced glass-forming ability induced by Cu-addition. These structural and compositional differences lead to a clear distinction in critical exponents near phase transitions between the Cu-free and Cu-added alloys, as well as a significantly lower peak value of magnetic entropy change for the Cu-free alloy ( $9.2 \text{ J kg}^{-1} \text{ K}^{-1}$  ( $5 \text{ T}$ )) compared to Cu-added alloys ( $10.8$ – $11.1 \text{ J kg}^{-1} \text{ K}^{-1}$  ( $5 \text{ T}$ )). The Cu-added alloys possess the comparable magnetocaloric properties to those of the reported rare-earth-containing high-entropy-metallic-glasses with similar transition temperatures. The designed Cu-added GdHoErNi HEAs exhibit a great potential as high-performance magnetic refrigerants suitable for hydrogen liquefaction applications.

## 1. Introduction

In comparison to traditional gas compression refrigeration, magnetic refrigeration (MR) based on magnetocaloric effect (MCE) has emerged as a current research hotspot, owing to its merits such as high efficiency, stability, and environmental friendliness [1–4]. Consequently, MR is widely considered to be the next generation of refrigeration technology [5]. The key of MR technology lies in the exploration of magnetocaloric materials, which are suitable for refrigeration cycles with high MCE performance in the targeted temperature range. Sustainable hydrogen energy is a cornerstone of climate-neutrality. Hydrogen liquefaction is important for efficiently storing and transporting hydrogen energy [6, 7]. Therefore, if pre-cooled by liquid nitrogen, it is of great significance to explore magnetocaloric materials working in the temperature range required by hydrogen liquefaction, i.e.,  $20$ – $77$  K [7].

In recent years, materials with giant MCE, e.g.  $\text{GdSiGe}$  [8],  $\text{LaFeCoSi}$  [9],  $\text{MnFePAs}$  [10], and  $\text{NiMnGa}$  [11], have been developed. The high magnetic entropy changes ( $|\Delta S_M|$ ) of these materials are attributed to

their first-order magnetic transitions (FOMT). However, the noticeable magnetic and thermal hysteresis induced by FOMT, and narrow working temperature span hinder the application of these materials. In contrast, materials undergoing second-order magnetic transitions (SOMT) exhibit comparable MCE properties, negligible magnetic and thermal hysteresis, and broad working temperature spans [12]. Therefore, SOMT materials have attracted considerable attention recently. Among the SOMT materials, rare-earth (RE) containing alloys show the relatively high  $|\Delta S_M|$ , which is ascribed to the highly effective magnetic moments of the RE elements [13]. Most research related with SOMT materials focuses on the alloys with an amorphous or crystalline structure [3,13,14]. Wang et al. stated that  $\text{Gd}_{34}\text{Ni}_{33}\text{Al}_{33}$  metallic glass exhibited the Curie temperature ( $T_C$ ) of  $38$  K and peak value of magnetic entropy change ( $|\Delta S_M^{\text{pk}}|$ ) of  $11.06 \text{ J kg}^{-1} \text{ K}^{-1}$  under a magnetic field change ( $\mu_0 \Delta H$ ) of  $5 \text{ T}$  [15]. The  $\text{Er}_{60}\text{Cu}_{20}\text{Al}_{20}$  amorphous alloy was explored. This alloy showed a  $|\Delta S_M^{\text{pk}}|$  of  $12.2 \text{ J kg}^{-1} \text{ K}^{-1}$  at  $\mu_0 \Delta H = 5 \text{ T}$  and  $T_C$  of  $13.3 \text{ K}$  [16]. The distances between magnetic atoms in amorphous alloy are longer

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than those in crystalline alloys with the same compositions, which is due to the homogenous structure of amorphous alloys [17]. Non-magnetic elements like Al or Cu are often employed to enhance the glass-forming ability (GFA) of RE-containing amorphous alloys [15,16,18]. These atoms tend to occupy the positions isolating the magnetic atoms in RE-containing amorphous alloys [17]. These lead to promising applications for RE-containing amorphous alloys at cryogenic temperatures, especially in hydrogen liquefaction temperature range [3]. In addition, due to the disorder structure, the amorphous alloys possess the superior mechanical and corrosion resistance properties [19,20], making them suitable for refrigeration cycles. In the field of crystalline alloys, high-entropy alloys (HEAs), as a new class of alloy system, have been developed rapidly in recent years [4,14].

Unlike conventional alloys, HEAs involve multiple primary elements ( $\geq 4$ ), providing an extensive compositional design space [21–23]. Yuan et al. [14] reported that the transition temperatures for  $\text{Tb}_{25}\text{Dy}_{25}\text{Ho}_{25}\text{Er}_{25}$ ,  $\text{Gd}_{25}\text{Tb}_{25}\text{Ho}_{25}\text{Er}_{25}$ , and  $\text{Gd}_{20}\text{Tb}_{20}\text{Dy}_{20}\text{Ho}_{20}\text{Er}_{20}$  alloys are 52, 139 and 186 K, respectively. The transition temperature of RE-containing alloys is commonly proportional to the deGennes factor of RE elements. Starting from Gd, the deGennes factor of elements decreases with increasing atomic number [24]. From the above results, it can be inferred that the design concept of multiple major RE elements could tune the magnetic transition temperature of the RE-containing HEA to the desired temperature range. Additionally, they found that  $\text{Gd}_{20}\text{Tb}_{20}\text{Dy}_{20}\text{Ho}_{20}\text{Er}_{20}$  alloy exhibited the relatively high  $|\Delta S_{\text{M}}^{\text{pk}}|$  of  $8.6 \text{ J kg}^{-1} \text{ K}^{-1}$ , wide working temperature span, and resultant high refrigerant capacity (RC) of  $627 \text{ J kg}^{-1}$  at  $\mu_0\Delta H = 5 \text{ T}$ . The high mixing entropy ( $\Delta S_{\text{mix}}$ ) in HEAs leads to chemical disorder, hindering the ordered arrangement of magnetic moments, thus causing slow rotation of magnetic moments during the phase transition. This broadens their working temperature span and enhances the MCE properties.

As a combination of RE-containing amorphous alloys and HEAs, RE-containing high-entropy-metallic-glasses (HE-MGs) exhibit both strong topological and chemical disorder, leading to improved MCE properties [4,25,26]. We [25] prepared the RE-containing HE-MGs with the compositions of  $\text{Gd}_{20}\text{Tb}_{20}\text{Dy}_{20}\text{Al}_{20}\text{TM}_{20}$  (TM = Co, Ni, and Fe). These alloys showed the  $|\Delta S_{\text{M}}^{\text{pk}}|$  in the range of  $5.96\text{--}9.43 \text{ J kg}^{-1} \text{ K}^{-1}$  and RC in the range of  $507\text{--}691 \text{ J kg}^{-1}$  at  $\mu_0\Delta H = 5 \text{ T}$ . However, it is unclear how the structure of HE-MGs contributes to the enhancement of the MCE performance. To address this issue, it is necessary to prepare RE-containing HE-MGs with different structures. The GFA is affected by atomic size difference ( $\delta$ ),  $\Delta S_{\text{mix}}$ , and mixing enthalpies ( $\Delta H_{\text{mix}}$ ). The enhancement of GFA is favored by larger  $\delta$ , higher  $\Delta S_{\text{mix}}$ , and higher absolute values of negative  $\Delta H_{\text{mix}}$  compared to solid solution alloys [27].

We noticed that Gd, Ho, and Er elements exhibit the relatively high magnetic moments [28]. In addition, the deGennes factor of Gd differs significantly from that of Ho and Er. Therefore, when these elements are all major constituents, according to the rule of mixture, it is highly probable that the working temperature range of the alloy would be within the temperature range required by hydrogen liquefaction (20–77 K) [29]. Based on the above compositional design principles, Zhang et al. [30] designed the HE-MG of  $\text{Gd}_{20}\text{Ho}_{20}\text{Er}_{20}\text{Ni}_{20}\text{Cu}_{20}$  with  $T_{\text{C}}$  of 41 K and  $|\Delta S_{\text{M}}^{\text{pk}}|$  of  $12 \text{ J kg}^{-1} \text{ K}^{-1}$  at  $\mu_0\Delta H = 5 \text{ T}$ .

The atomic size of Cu is smaller than that of RE elements. The heat of mixing for the atom pairs between Cu and RE elements are large and negative. Therefore, adding Cu in compositional design of RE-containing HEAs is beneficial for increasing their  $\delta$  and the absolute value of negative  $\Delta H_{\text{mix}}$ . Reducing the number of elements, such as from five to four, can decrease the  $\Delta S_{\text{mix}}$  of the alloys. Mo et al. [31] and our previous work [18] found that Cu element is beneficial for enhancing the MCE properties of RE-containing alloys. Therefore, aiming to achieve the transformation of the RE-containing HEA from a crystalline or crystalline-containing structure to a fully amorphous structure, we chose to tune the Cu content in the  $\text{Gd}_{20}\text{Ho}_{20}\text{Er}_{20}\text{Ni}_{20}\text{Cu}_{20}$  alloy to control its GFA.

The morphology of magnetocaloric materials significantly influences their properties and practical applications. Magnetocaloric materials typically exist in four different shapes: bulk, ribbon, microwire, and powder. Bulk materials, characterized by a small specific surface area, exhibit low heat transfer efficiency, whereas powders, despite their large specific surface area, suffer from a nonnegligible pressure drop, which limits their applicability in magnetic refrigerators [32,33]. In contrast, ribbons and microwires combine high specific surface areas with excellent mechanical strength, making them more suitable for practical cooling devices [32,33]. Recent studies have demonstrated that ribbons [12,15,16,18,26,30,34–42] and microwires [43–55], which are also applicable in chemical and environmental sciences [56], possess excellent MCE.

In this study, we designed the HEA compositions of  $(\text{Gd}_{25}\text{Ho}_{25}\text{Er}_{25}\text{Ni}_{25})_{100-x}\text{Cu}_x$  ( $x = 0, 10, \text{ and } 20$ ). These alloys were processed into ribbon forms. The alloys without and with Cu addition show the amorphous/nanocrystalline dual-phase structure and fully amorphous structure, respectively. All elements are evenly distributed, except for the enrichment of Ni in the minor amorphous phase of the Cu-free alloy. The  $T_{\text{C}}$  of the studied alloys are in the temperature range of 41–45 K. Compared with the Cu-free alloy, the Cu-added alloys exhibit the higher  $|\Delta S_{\text{M}}^{\text{pk}}|$ , i.e.,  $10.8\text{--}11.1 \text{ J kg}^{-1} \text{ K}^{-1}$  at  $\mu_0\Delta H = 5 \text{ T}$ . The Cu-added alloys exhibit the comparable magnetocaloric properties to those of the reported RE-containing HE-MGs with the similar transition temperatures.

## 2. Experimental details

The master alloys with the nominal compositions of  $(\text{Gd}_{25}\text{Ho}_{25}\text{Er}_{25}\text{Ni}_{25})_{100-x}\text{Cu}_x$  ( $x = 0, 10, \text{ and } 20$ ) were prepared by arc melting the mixtures of commercial-grade metals with purities higher than 99.9 wt%. These alloys are hereafter referred to as Cu0, Cu10, and Cu20, respectively. This fabrication procedure was performed under a Ti-gettered argon atmosphere. To achieve high chemical uniformity, each pre-alloyed ingot was remelted five times. After the arc melting process, the mass losses of the ingots were less than 0.5 %. Subsequently, the ingots were put into the melt-spinning equipment. The alloy ribbons were obtained by dropping the melt onto a spinning Cu roller with a surface velocity of 45 m/s. The thicknesses of Cu0, Cu10 and Cu20 ribbons are about 47, 29, and 25  $\mu\text{m}$ , respectively. The structure of the ribbons was preliminarily examined by an X-ray diffraction (XRD, Bruker D8 Advance) over a  $2\theta$  range of  $20^\circ$  to  $80^\circ$ . The thermal analysis for the ribbons was carried out by a differential scanning calorimetry (DSC) from room temperature to 1250 K at a heating rate of  $40 \text{ K min}^{-1}$  (Netzsch DSC-404-C). The transmission electron microscopy (TEM, Thermo Fisher Talos F200x) equipped with energy-dispersive X-ray spectroscopy (EDS) was used to observe the nanoscale microstructure of the ribbons. The magnetic and magnetocaloric behavior was determined by a Magnetic Property Measurement System (MPMS, Quantum Design SQUID-VSM). The field-cooled (FC) and zero-field-cooled (ZFC) magnetization ( $M$ )-temperature ( $T$ ) curves were tested under a magnetic field of 0.02 T. The measurements of the isothermal  $M$ - $H$  curves were conducted from 100 K to 10 K. Each curve was measured from 0 to 5 T. The interval of the test temperature was 5 K.

## 3. Results and discussion

Fig. 1 shows the XRD patterns for Cu0, Cu10 and Cu20 alloys. The XRD pattern for Cu0 alloy exhibits the clearly sharp Bragg peaks, indicating the presence of crystalline phase. The structure of the crystalline phase is confirmed as hexagonal close-packed (HCP). The broad and diffused peaks of the Cu10 and Cu20 alloys indicate the fully amorphous structure of these alloys.

The DSC curves for Cu0, Cu10 and Cu20 alloys are displayed in Fig. 2. The exothermic peaks on all DSC curves in the temperature range

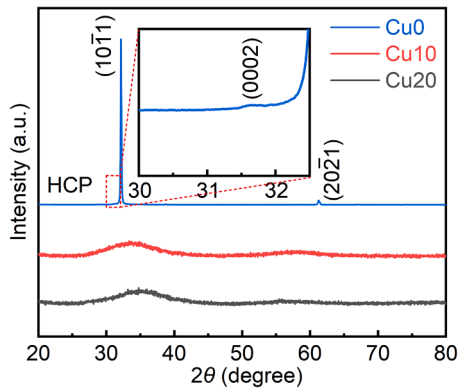


Fig. 1. XRD patterns for the Cu0, Cu10 and Cu20 alloys.

of 500–650 K confirm the crystallization of the amorphous phase for all alloys, as shown in Fig. 2a. This determines the existence of the amorphous phase for all studied alloys. The DSC curves for Cu10 and Cu20 alloys possess the endothermic peaks in the temperature range of 500–600 K, corresponding to the glass transition region. As shown in Fig. 2b, all curves exhibit the melting region, i.e., endothermic peaks in the temperature range above 950 K. The glass transition temperature ( $T_g$ ), crystallization temperature ( $T_x$ ), and liquidus temperature ( $T_l$ ) are labeled in Fig. 2 and listed in Table 1. The absence of endothermic peaks in the temperature range below  $T_x$  results in  $T_g$  not being identifiable in the DSC curve of Cu0 alloy. The criteria for GFA, i.e., the reduced glass transition temperature ( $T_{rg}$ ) and parameter  $\gamma$ , can be obtained as follows:  $T_{rg} = T_g/T_l$  [57,58], and  $\gamma = T_x/(T_g+T_l)$  [59], respectively. The width of supercooled liquid region ( $\Delta T_x$ ) is calculated as  $\Delta T_x = T_x - T_g$  [34], which reflects the ability for hindering the crystallization of the amorphous alloy. Table 1 shows the  $T_{rg}$ ,  $\gamma$ , and  $\Delta T_x$  of Cu10 and Cu20 alloys. The  $T_{rg}$ ,  $\gamma$ , and  $\Delta T_x$  of Cu10 and Cu20 alloys are relatively high compared with those of reported MCE amorphous alloys [35–38]. Guo et al. proposed a criterion for HE-MG, i.e.,  $\delta \geq 9$ ,  $-49 \leq \Delta H_{mix} \leq -5.5 \text{ kJ mol}^{-1}$  and  $7 \leq \Delta S_{mix} \leq 16 \text{ J K}^{-1} \text{ mol}^{-1}$  [27]. As listed in Table 1, these parameters for the Cu0, Cu10 and Cu20 alloys are in accordance with this criterion. With increasing Cu content, the absolute values of  $\delta$ ,  $\Delta S_{mix}$ , and  $\Delta H_{mix}$  increase, resulting in the relatively high GFA of Cu10 and Cu20 alloys.

TEM observations were used for analyzing the nanoscale microstructures of Cu0, Cu10, Cu20 alloys. The bright-field TEM image shows

the numerous nanocrystals existing in the Cu0 alloy, as shown in Fig. 3a. The high-resolution TEM (HRTEM) image, Fig. 3b, confirms the amorphous/nanocrystalline dual-phase structure of the Cu0 alloy. This explains that the crystallization of the amorphous phase leads to the exothermic peak of the Cu0 alloy in Fig. 2a. Fig. 3c displays the fast Fourier transform (FFT) result corresponding to the red dashed squares in Fig. 3b. The HCP structure of the nanocrystalline phase in the Cu0 alloy is determined by its FFT result and diffraction rings in the selected area electron diffraction (SAED) pattern shown in Fig. 3d. The absence of information regarding the amorphous phase structure in the XRD results of the Cu0 alloy may be attributed to the limitations of the XRD equipment in detecting phases with low fractions [44]. The absence of  $T_g$  in the DSC curve of Cu0 alloy is a common phenomenon in the DSC curves of the amorphous/nanocrystalline dual-phase alloys [60,61]. The HRTEM images of Cu10 and Cu20 alloys (Fig. 3e and f) show the homogeneous maze-like patterns. In the insets of Fig. 3e and f, the SAED patterns exhibit the rather faint and diffused halo rings without any noticeable diffraction spot. These results confirm the fully amorphous structure of Cu10 and Cu20 alloys [62], in agreement with the analysis results of their XRD and DSC results. We successfully tune the structure of RE-containing HEA from crystalline-containing structure to fully amorphous structure through the compositional design. The fully amorphous structure of Cu10 and Cu20 alloys is attributed to (i) their relatively high  $T_{rg}$ ,  $\gamma$ , and  $\Delta T_x$  and (ii) their much smaller ribbon thicknesses compared with the calculated critical section thickness ( $Z_c = 2.80 \times 10^{-7} \exp(41.70 \times \gamma)$  [59]), i.e., 355 and 190  $\mu\text{m}$  for Cu10 and Cu20, respectively.

Fig. 4 presents the high-angle-annular-dark-field (HAADF) images and the EDS mapping results of the Cu0, Cu10 and Cu20 alloys. In Cu0 alloy, the RE elements are uniformly dispersed, with an enrichment of Ni element within the amorphous phase. This is consistent with the compositional difference between amorphous phase and nanocrystalline phase of other RE-transition-metal-element amorphous alloys [63]. The deep eutectic compositions enhance the GFA [64]. Among the elements composing the Cu0 alloy, only RE and Ni elements can form the deep eutectic systems, thereby leading to the formation of a Ni-rich amorphous phase in the Cu0 alloy. All elements are homogeneously distributed in Cu10 and Cu20 alloys.

Fig. 5a displays the FC and ZFC  $M-T$  curves for Cu0, Cu10 and Cu20 alloys. Based on the FC  $M-T$  curves, the  $dM/dT-T$  curves for the studied alloys are calculated and shown in the inset of Fig. 5a. The  $T_C$  of the Cu0,

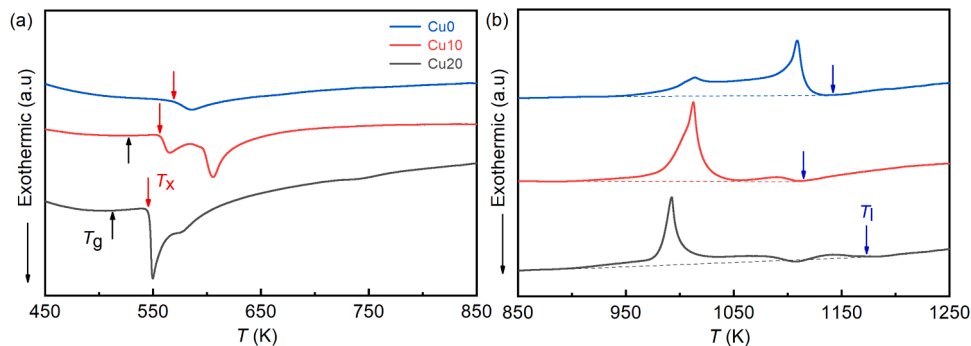


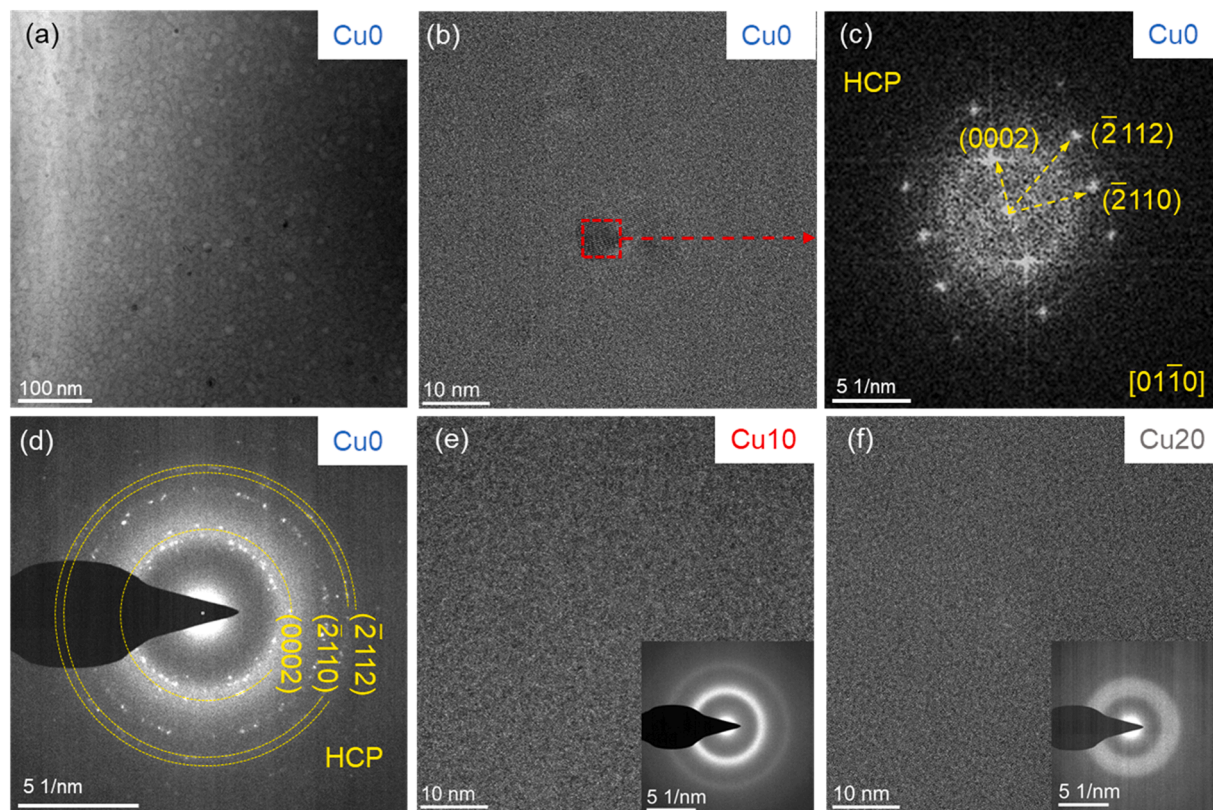
Fig. 2. DSC curves for the Cu0, Cu10 and Cu20 alloys. (a) 450–850 K; (b) 850–1250 K.

Table 1

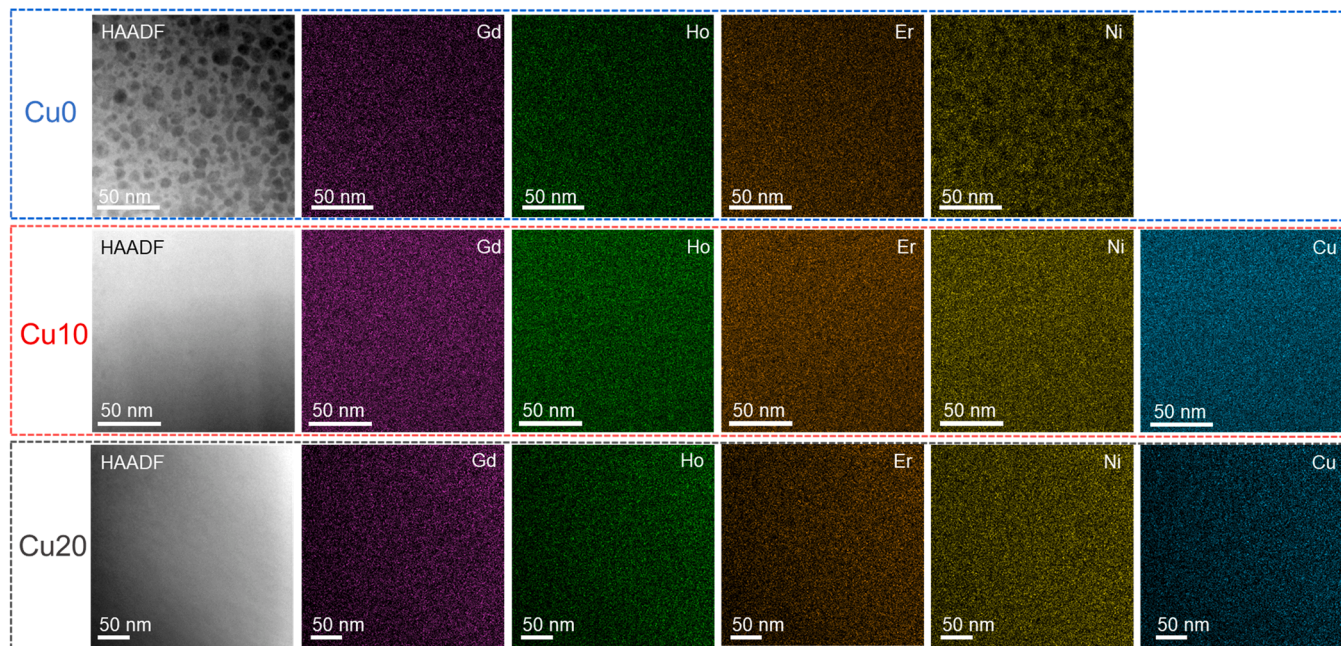
The thermophysical parameters of the Cu0, Cu10 and Cu20 alloys.

Sample	$T_g$ (K)	$T_x$ (K)	$T_l$ (K)	$\Delta T_x$ (K)	$T_{rg}$	$\gamma$	$\delta$	$\Delta H_{mix}$ (kJ mol <sup>-1</sup> )	$\Delta S_{mix}$ (J K <sup>-1</sup> mol <sup>-1</sup> )
Cu0	-	569	1157	-	-	-	13.97	-24	11.53
Cu10	527	556	1114	29	0.473	0.339	15.16	-25.47	13.08
Cu20	513	546	1173	33	0.437	0.322	16.03	-26.08	13.38





**Fig. 3.** (a) The bright-field TEM image of Cu0 alloy. (b) and (c) HRTEM images and FFT results corresponding to the red dashed squares in HRTEM images of Cu0 alloy, respectively. (d) the corresponding SAED results of Cu0 alloy. (e) and (f) HRTEM images and corresponding SAED results (insets) of Cu10 and Cu20 alloys, respectively.

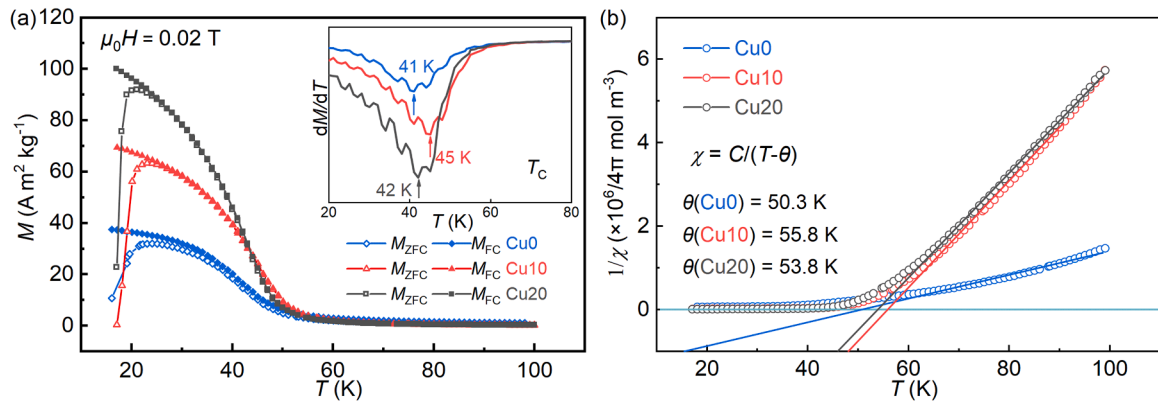


**Fig. 4.** The HAADF images and the EDS mapping results of the Cu0, Cu10 and Cu20 alloys.

Cu10 and Cu20 alloys is determined to be 41, 45, and 42 K, respectively, corresponding to the lowest points of the  $dM/dT$ - $T$  curves, as shown in the inset of Fig. 5a. The  $T_C$  for Cu0, Cu10 and Cu20 alloys is similar, which may be attributed to minimal impact of Cu addition on the  $T_C$  of the RE-containing alloys [31,65]. The FC and ZFC  $M$ - $T$  curves of the

studied alloys exhibit a distinct divergence at low temperature, indicating the typical spin-glass behavior [66–68]. In the spin-glass state, the magnetic moments are more difficult to rotate compared to those in the ferromagnetic state [26,39]. Therefore, the presence of the spin-glass phase can effectively broaden the working temperature span of





**Fig. 5.** (a) ZFC and FC  $M$ - $T$  curves for Cu0, Cu10 and Cu20 alloys under a magnetic field of 0.02 T. The inset shows the  $dM/dT$ - $T$  curves. (b) Temperature dependence of the inverse magnetic susceptibility and the linear fit for Cu0, Cu10 and Cu20 alloys.

magnetocaloric materials. The inverse magnetic susceptibility, i.e.,  $\chi^{-1} = \mu_0 H/M$ , derived from the  $M$ - $T$  curves is presented in Fig. 5b. By fitting the linear portion of the  $\chi^{-1}$ - $T$  curves, the obtained Curie-Weiss temperature ( $\theta_p$ ) are  $\theta_{p1} = 50.3$  K,  $\theta_{p2} = 55.8$  K, and  $\theta_{p3} = 53.8$  K, for Cu0, Cu10 and Cu20 alloys, respectively. The effective magnetic moment ( $\mu_{\text{eff}}$ ) can be obtained by [47]:  $\mu_{\text{eff}} = \sqrt{8C\mu_B}$ , where  $C$  is Curie constant. Based on the fitted straight lines, we obtained  $\mu_{\text{eff}} = 16.85 \mu_B$ ,  $7.90 \mu_B$ , and  $8.02 \mu_B$  for the Cu0, Cu10 and Cu20 alloys, respectively. The  $\mu_{\text{eff}}$  of Cu0 alloys is significantly larger than that of Cu10 and Cu20 alloys because Cu0 alloy contains intermetallic compounds rather than being simply amorphous [17]. For the Cu10 and Cu20 alloys, the  $\mu_{\text{eff}}$  increase with the addition of Cu. This increase is attributed to the reduction of antiferromagnetic exchange interactions between the 3d transition metal elements and the 4f rare earth elements (Ni and RE, RE = Gd, Ho, Er) caused by the addition of the nonmagnetic element Cu, leading to the observed increase in  $\mu_{\text{eff}}$  [47].

Fig. 6 shows the isothermal  $M$ - $\mu_0 H$  curves of Cu0, Cu10 and Cu20 alloys. At high temperature range, the magnetization increases linearly with the increase of applied magnetic field, indicating the paramagnetic state of the studied alloys. The ferromagnetic state of Cu0, Cu10 and Cu20 alloys at low temperatures is confirmed by a rapid increase in magnetization with increasing applied magnetic field, followed by a saturation. As the temperature decreases, the studied alloys possess the paramagnetic-ferromagnetic (PM-FM) transition.

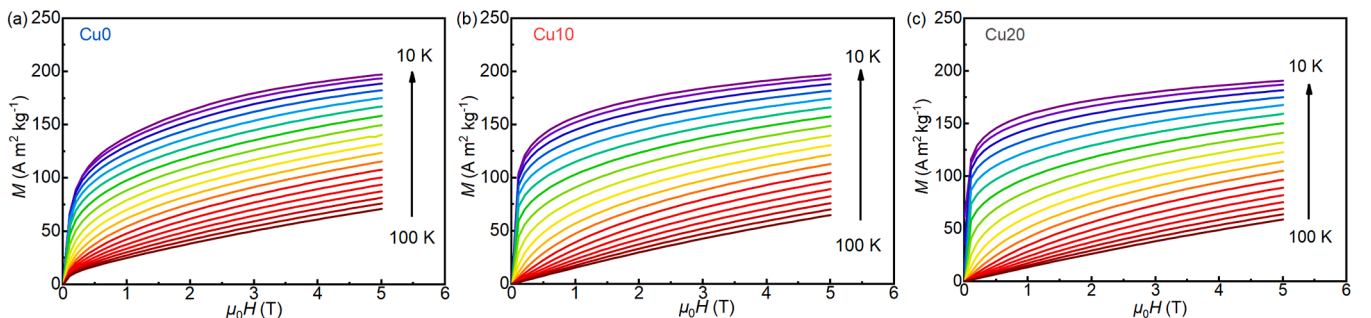
To determine the magnetic transition types of Cu0, Cu10 and Cu20 alloys, Arrott plots were obtained based on the  $M$ - $\mu_0 H$  curves, as shown in Fig. 7. According to the Banerjee criterion [69], as the slope of the Arrott plots is negative, the magnetic transition type is identified as a FOMT. Conversely, the SOMT can be confirmed by the positive slope of Arrott plots. All Arrott plots for Cu0, Cu10 and Cu20 alloys show positive slopes, suggesting the presence of SOMT in these alloys. Due to the limitation of the Arrott plots in determining magnetic transition types of MCE materials [70], additional methods have been applied to analyze

magnetic transition types of the studied alloys. The relevant results are presented in the subsequent sections. According to the Maxwell relation, the  $\Delta S_M$  of magnetic materials can be obtained based on the isothermal  $M$ - $\mu_0 H$  curves and the integral method [13]:

$$\Delta S_M = \mu_0 \int_0^{H_{\text{max}}} (\partial M / \partial T) dH$$

$$= \mu_0 \left( \int_0^H M(T_i, H) dH - \int_0^H M(T_{i+1}, H) dH \right) / (T_i - T_{i+1}) \quad (1)$$

where  $\mu_0 H_{\text{max}}$  is the maximum value of the applied magnetic field. Fig. 8 shows the  $|\Delta S_M|$  as a function of temperature at various  $\mu_0 \Delta H$  for Cu0, Cu10 and Cu20 alloys. As shown in Fig. 8a-c, the  $|\Delta S_M^{\text{pk}}|$  is 9.2, 10.8, and 11.1 J kg<sup>-1</sup> K<sup>-1</sup> for Cu0, Cu10 and Cu20 alloys, respectively, at  $\mu_0 \Delta H = 5$  T. The  $|\Delta S_M^{\text{pk}}|$  of Cu20 alloy is close to that of the reported alloy with the same composition, i.e., 12 J kg<sup>-1</sup> K<sup>-1</sup> at  $\mu_0 \Delta H = 5$  T [30]. In addition, all  $|\Delta S_M|$ - $T$  curves show the working temperature ranges covering the temperature range of 20–77 K. This indicates success of our compositional design for the RE-containing HE-MG working in the temperature range required by hydrogen liquefaction. Fig. 8d displays the  $|\Delta S_M|$ - $T$  curves of Cu0, Cu10 and Cu20 alloys at  $\mu_0 \Delta H = 5$  T. The Cu10 and Cu20 alloys possess the similar and relatively high  $|\Delta S_M|$  compared with that of Cu0 alloy. The addition of Cu gradually increases the  $|\Delta S_M^{\text{pk}}|$ . This increase in isothermal  $|\Delta S_M|$  arises from the interplay between the competition of ferromagnetic (FM) and antiferromagnetic (AFM) exchange interactions among the elements and the magnetic dilution effect of Cu [47,52]. As a non-magnetic element, Cu increases the RE-RE (RE = Gd, Ho, Er) distance when incorporated into the alloy, thereby diluting the FM RE-RE exchange interactions [52]. With increasing Cu content, the Ni content decreases, leading to a reduction in the RE-Ni AFM interactions. These result in an increase in the  $|\Delta S_M^{\text{pk}}|$  with higher Cu content [47,52]. In addition, the adiabatic temperature change ( $\Delta T_{\text{ad}}$ ) under a magnetic field variation can be determined



**Fig. 6.** Isothermal  $M$ - $\mu_0 H$  curves at 0–5 T. (a) Cu0; (b) Cu10; (c) Cu20.

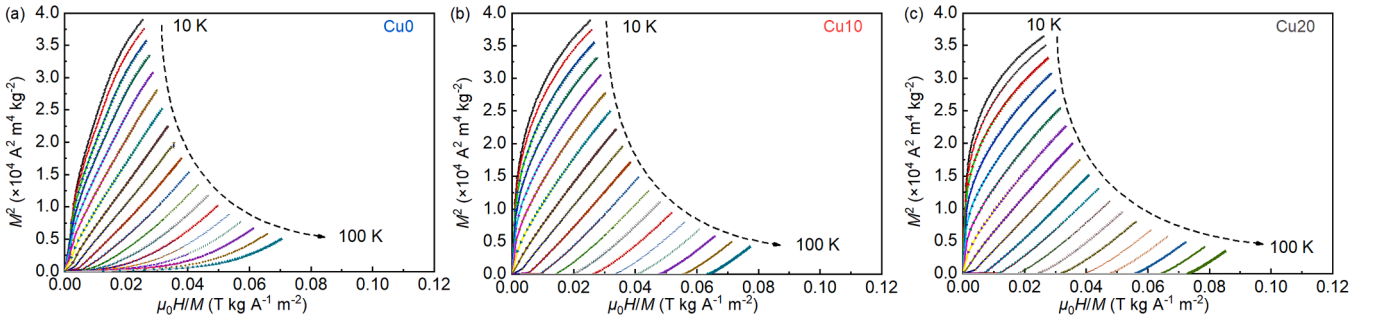


Fig. 7. Arrott plots obtained based on isothermal  $M$ - $\mu_0 H$  curves. (a) Cu0; (b) Cu10; (c) Cu20.

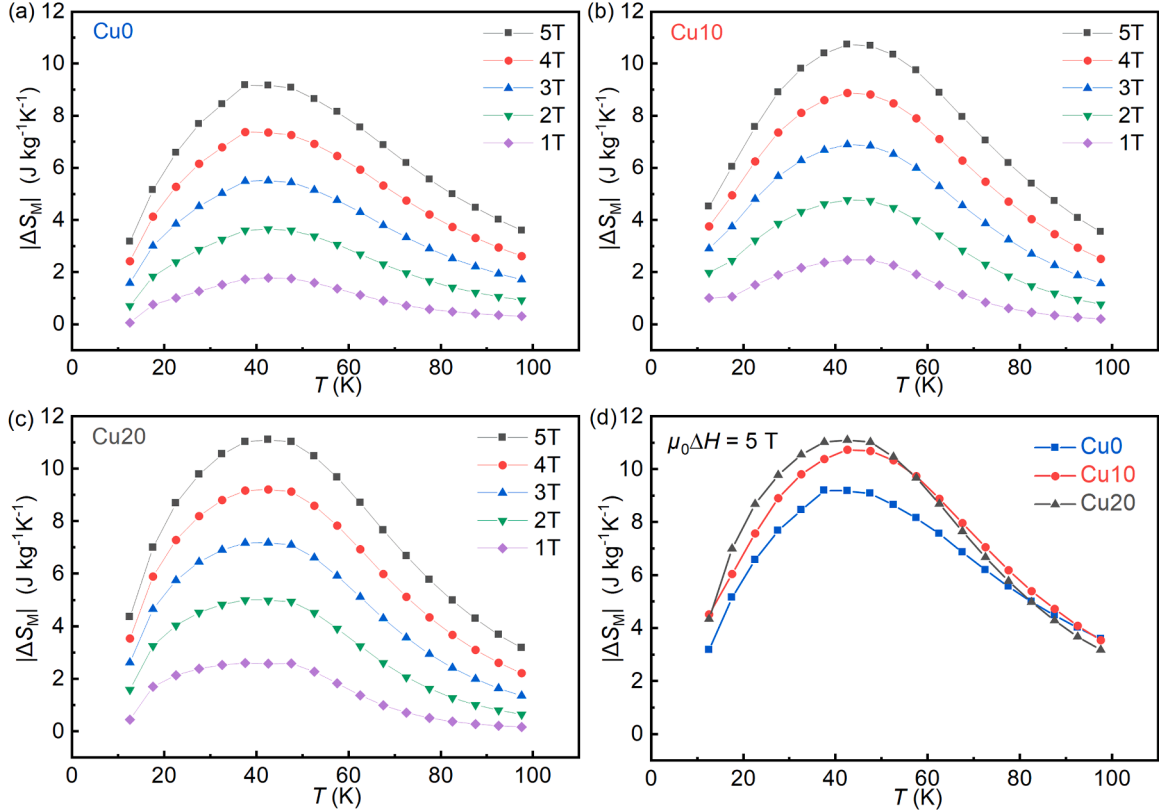


Fig. 8.  $|\Delta S_M|$ - $T$  curves of (a) Cu0, (b) Cu10, and (c) Cu20 alloys at  $\mu_0 \Delta H = 1$ –5 T. (d)  $|\Delta S_M|$ - $T$  curves for all studied alloys at  $\mu_0 \Delta H = 5$  T.

indirectly from the measured magnetization and the temperature dependence of heat capacity ( $C_p(T)$ ) at 0 T [71]:

$$\Delta T_{ad}(T, H) = T/C_p(T) * \Delta S_M(T, H) \quad (2)$$

By this method, the  $\Delta T_{ad}$  of the Cu20 alloy under field changes of 1 T, 2 T, 3 T, 4 T and 5 T is shown in Fig. 9, the inset of which shows the temperature dependence of heat capacity at 0 T. The maximum values of  $\Delta T_{ad}$  are determined to be 0.83, 1.59, 2.29, 2.95 and 3.59 K under field changes of 1, 2, 3, 4 and 5 T, respectively. These values are comparable to previously reported Gd-based MG [72].

In addition to  $\Delta S_M$  and  $\Delta T_{ad}$ , another key parameter for evaluating the MCE properties is cooling efficiency, indirectly quantifying the amount of heat transferred in an ideal refrigeration cycle. The widely used cooling efficiency parameters are relative cooling power (RCP) and refrigeration capacity (RC) [73]. These parameters can be obtained as follows:

$$RCP = \left| \Delta S_M^{pk} \right| \times \Delta T_{FWHM} = \left| \Delta S_M^{pk} \right| (T_2 - T_1) \quad (3)$$

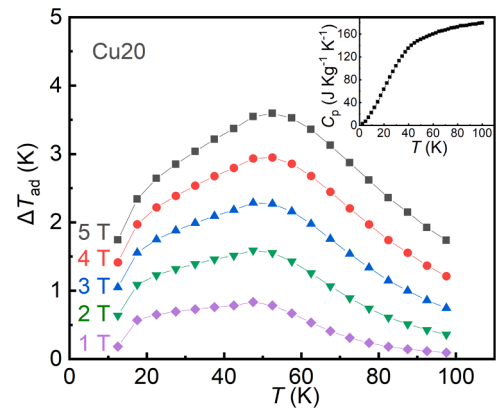


Fig. 9. The adiabatic temperature change under field changes of 1 T, 2 T, 3 T, 4 T and 5 T for the Cu20 alloy measured at temperatures between 10 and 100 K. The inset shows the temperature dependence of heat capacity at 0 T.



$$RC = \int_{T_1}^{T_2} |\Delta S_M(T)| dT \quad (4)$$

where  $T_1$  and  $T_2$  represent the initial and final temperatures, respectively, corresponding to the full-width at half-maximum of the  $|\Delta S_M|$ - $T$  curve ( $\Delta T_{FWHM}$ ), i.e., working temperature span. The magnetocaloric parameters for Cu0, Cu10 and Cu20 alloys are listed in Table 2. The  $\Delta T_{FWHM}$  for the Cu0, Cu10 and Cu20 alloys is 70.4 K, 67.5 K, and 64.2 K, respectively. The strong competition between FM and AFM interactions and spin-glass phase results in the largest  $\Delta T_{FWHM}$  for Cu0 [47]. While the addition of Cu in Cu10 and Cu20 reduces AFM interactions, the competition between FM and AFM still exists, leading to relatively large  $\Delta T_{FWHM}$ . However, the higher  $|\Delta S_M|$  of Cu10 and Cu20 compensates for their smaller  $\Delta T_{FWHM}$ , resulting in their relatively large RC.

The formula of  $|\Delta S_M| \propto (\mu_0 \Delta H)^n$  is commonly used to describe the relationship between  $|\Delta S_M|$  and  $\mu_0 \Delta H$  [74]. Exponent  $n$  is simultaneously related to the temperature and magnetic field change. The local value of exponent  $n$  can be obtained by the following equation:

$$n = d \ln |\Delta S_M| / d \ln |\mu_0 \Delta H| \quad (5)$$

Fig. 10a shows the  $n$ - $T$  curves at  $\mu_0 \Delta H = 5$  T for Cu0, Cu10 and Cu20 alloys. In the whole temperature range, all  $n$ - $T$  curves are below 2, confirming the SOMET of Cu0, Cu10 and Cu20 alloys [75,76]. The presence of only one phase transition feature in the  $|\Delta S_M|$ - $T$  and  $n$ - $T$  curves of Cu0 alloy, as shown in Fig. 8a and d, and Fig. 10a, may be attributed to its amorphous phase with low fraction [77].

The rescaled curve is another widely used method to analyze the magnetic transition type of the MCE materials [75,78]. Based on the  $|\Delta S_M|$ - $T$  curves, the y-axis of the rescaled curves is obtained by  $\Delta S_M / \Delta S_M^{\text{pk}}$ . The temperature of the magnetocaloric curves is normalized to a dimensionless axis ( $\theta$ ), i.e., x-axis of the rescaled curves, by the following equation [74]:

$$\theta = \begin{cases} -(T - T_{\text{peak}}) / (T_{r1} - T_{\text{peak}}); & T \text{ and } T_{r1} \leq T_{\text{peak}} \\ (T - T_{\text{peak}}) / (T_{r2} - T_{\text{peak}}); & T \text{ and } T_{r2} > T_{\text{peak}} \end{cases} \quad (6)$$

where  $T_{\text{peak}}$  represents the temperature corresponding to  $|\Delta S_M^{\text{pk}}|$ ,  $T_{r1}$  and  $T_{r2}$  represent reference temperatures corresponding to  $\Delta S_M(T_{r1}) = \Delta S_M(T_{r2}) = 0.7 \Delta S_M^{\text{pk}}$ . Fig. 10b-d show the rescaled curves of the Cu0, Cu10 and Cu20 alloys at  $\mu_0 \Delta H = 2$ -5 T, respectively. The rescaled curves for Cu10 alloy collapse well onto a single universal curve, confirming the SOMET in this alloy [75]. For Cu0 and Cu20 alloys, although there is relatively poor overlap in their rescaled curves, the degree of dispersion is within the acceptable range of using the rescaled curves to determine the SOMET [70]. Therefore, both Cu0 and Cu20 alloys exhibit SOMET within the test temperature range.

The  $\mu_0 \Delta H$  dependence of  $|\Delta S_M^{\text{pk}}|$  follows the power-law relationship [79]:

**Table 2**

The  $T_C$ ,  $|\Delta S_M^{\text{pk}}|$ , and RC at  $\mu_0 \Delta H = 5$  T for Cu0, Cu10, Cu20 alloys, and reported RE-containing HE-MGs working in hydrogen liquefaction temperature.

Sample	$T_C$ (K)	$\mu_0 \Delta H$ (T)	$ \Delta S_M^{\text{pk}} $ (J kg <sup>-1</sup> K <sup>-1</sup> )	RC (J kg <sup>-1</sup> )	Refs.
Cu0	41	5	9.2	518	This work
Cu10	45	5	10.8	585	This work
Cu20	42	5	11.1	585	This work
Gd <sub>20</sub> Ho <sub>20</sub> Er <sub>20</sub> Ni <sub>20</sub> Cu <sub>20</sub>	41	5	12	640.8	[30]
Dy <sub>36</sub> Ho <sub>20</sub> Al <sub>24</sub> Co <sub>20</sub>	23	5	9.49	326	[93]
Gd <sub>18</sub> Ho <sub>22</sub> Tm <sub>20</sub> Cu <sub>22</sub> Al <sub>18</sub>	33.6	5	8.7	401.8	[40]
Gd <sub>25</sub> Co <sub>25</sub> Al <sub>25</sub> Ho <sub>20</sub> Y <sub>5</sub>	49	5	8.79	547	[41]
Gd <sub>20</sub> Tb <sub>20</sub> Dy <sub>20</sub> Al <sub>20</sub> Ni <sub>20</sub>	45	5	7.25	507	[25]
Er <sub>20</sub> Dy <sub>20</sub> Co <sub>20</sub> Al <sub>20</sub> Tb <sub>20</sub>	29	5	8.6	525	[67]
Gd <sub>20</sub> Ho <sub>20</sub> Er <sub>20</sub> Al <sub>20</sub> Ni <sub>20</sub>	25	5	9.5	511	[94]
Sm <sub>20</sub> Gd <sub>20</sub> Dy <sub>20</sub> Co <sub>20</sub> Al <sub>20</sub>	52	5	6.34	322.9	[95]
Gd <sub>20</sub> Ho <sub>20</sub> Tm <sub>20</sub> Cu <sub>20</sub> Ni <sub>20</sub>	32	5	10.6	528	[42]

$$|\Delta S_M^{\text{pk}}| = a(\mu_0 \Delta H)^b \quad (7)$$

where  $a$  and  $b$  represent constants. Fig. 11 shows the  $|\Delta S_M^{\text{pk}}|$ - $\mu_0 \Delta H$  curves and the fitting results by using Eq. (7). The results of exponent  $b$  and determination coefficients of the fitting ( $R^2$ ) are listed in Table 3. The values of  $R^2$  close to 1 indicate the good fitting. This indicates that all studied alloys exhibit SOMET [74,80], which is consistent with the analysis results of the  $n$ - $T$  curves, rescaled curves, and Arrott plots. Both  $n$  around  $T_C$  and exponent  $b$  for alloys with SOMET are associated with the critical exponents [75,79,81]. As shown in Fig. 10a and Table 3, the  $n$  around  $T_C$  and exponent  $b$  for Cu10 and Cu20 alloys are close, which are lower than those of Cu0 alloy. This indicates the critical behavior of Cu0 alloy is different from that of Cu10 and Cu20 alloys. Due to the absence of Ni elements, there is a significant difference in composition between the nanocrystalline phase of the Cu0 alloy and the amorphous phases of the Cu10 and Cu20 alloys. This, combining the structural difference between nanocrystalline and amorphous phases, leads to a significant disparity in the critical exponents between the nanocrystalline phase of the Cu0 alloy and the amorphous phases of the Cu10 and Cu20 alloys [47,52,82,83]. The critical exponents of the amorphous phases for RE-containing HE-MGs are insensitive to compositional changes [82]. Therefore, Cu10 and Cu20 alloys with fully amorphous structures possess the similar critical exponents.

In SOMET materials, the critical behavior of the FM-PM phase transition is characterized by three critical exponents,  $\beta$ ,  $\gamma$ , and  $\delta$  [84], which are correlated with the magnetocaloric behavior of SOMET materials [52, 85–87]. These exponents are associated with the spontaneous magnetization  $M_S(T)$ , the thermal dependence of the initial inverse susceptibility  $\chi_0^{-1}(T)$ , and the field dependence of the magnetization of the critical isotherm, respectively [84]. Their values can be defined by using the following power-law relations:

$$M_S(T) = M_0(-\varepsilon)^\beta; \quad \varepsilon < 0, \quad T < T_C \quad (8)$$

$$\chi_0^{-1}(T) = (H_0/M_0)\varepsilon^\gamma; \quad \varepsilon > 0, \quad T > T_C \quad (9)$$

$$H = DM^\delta; \quad \varepsilon = 0, \quad T = T_C \quad (10)$$

where  $\varepsilon$  is the reduced temperature,  $\varepsilon = (T - T_C)/T_C$ , and  $H_0$ ,  $M_0$ ,  $D$  are the critical amplitudes.

According to the Arrott-Noakes equation of state [88]:

$$(H/M)^{1/\gamma} = A\varepsilon + BM^{1/\beta} \quad (11)$$

where  $A$  and  $B$  are material dependent parameters, the  $T_C$  for all alloys can be redefined by using modified Arrott plot (MAP) method. To use MAP approach, the  $M$ - $\mu_0 H$  data is reformulated, using initial values of  $\beta$  and  $\gamma$  and according to the Eq. (11). The accurate critical exponents are those that result in a linear relationship between  $M^{1/\beta}$  and  $(\mu_0 H/M)^{1/\gamma}$ , with  $T_C$  determined from the critical isotherm intersecting the origin. The initial values of  $\beta$  and  $\gamma$  can be estimated using one of the four theoretical models: the mean-field model, i.e.,  $\beta = 0.5$ ,  $\gamma = 1.0$ , the 3D Heisenberg model, i.e.,  $\beta = 0.365$ ,  $\gamma = 1.336$ , the 3D Ising model, i.e.,  $\beta = 0.325$ ,  $\gamma = 1.240$ , and the tricritical mean field model, i.e.,  $\beta = 0.25$ ,  $\gamma = 1$  [89,90]. The  $M_S(T)$  and the  $\chi_0^{-1}(T)$  were determined from the intercepts obtained by linearly extrapolating  $M^{1/\beta}$  and  $(\mu_0 H/M)^{1/\gamma}$ , respectively, using the high field isotherms of the MAPs. The critical exponents  $\beta$  and  $\gamma$  are obtained by fitting  $M_S(T)$  data to the relation  $M_S \propto (-\varepsilon)^\beta$  as described in Eq. (8) and the  $\chi_0^{-1}(T)$  data to the relation  $\chi_0^{-1} \propto (\varepsilon)^\gamma$  as given in Eq. (9). This process is iterated using the updated  $\beta$  and  $\gamma$  values until the isotherm passing through the origin corresponds to  $T = T_C$ , and the critical exponents  $\beta$  and  $\gamma$  converge to stable values. Fig. 12a-c presents the MAPs, in which the isotherms achieve good linearity with  $\beta_{\text{MAP}} = 0.641 \pm 0.003$ ,  $0.614 \pm 0.004$ ,  $0.566 \pm 0.005$ ,  $\gamma_{\text{MAP}} = 1.428 \pm 0.005$ ,  $1.381 \pm 0.003$ ,  $1.370 \pm 0.003$ , and  $T_{C\text{-MAP}}$

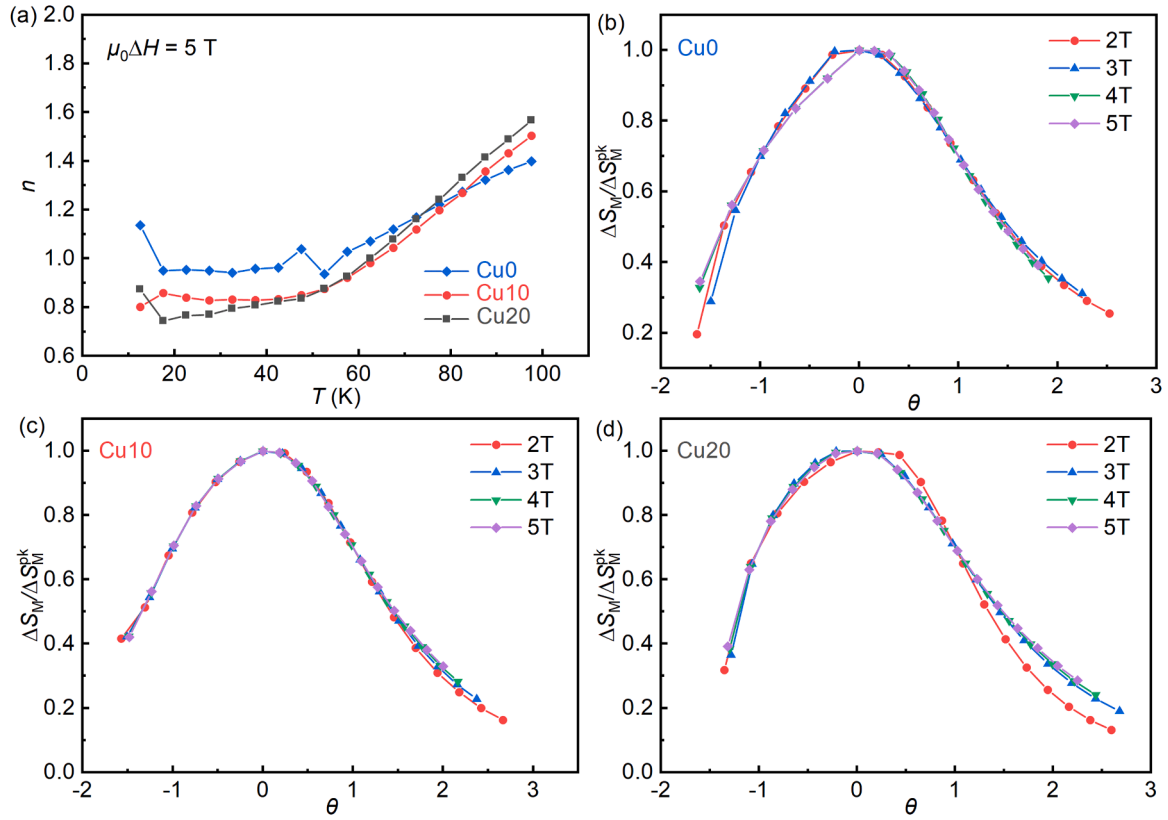


Fig. 10. (a) The  $n$ - $T$  curves at  $\mu_0\Delta H = 5$  T. The rescaled curves at  $\mu_0\Delta H = 2$ –5 T for the (b) Cu0, (c) Cu10, and (d) Cu20 alloys.

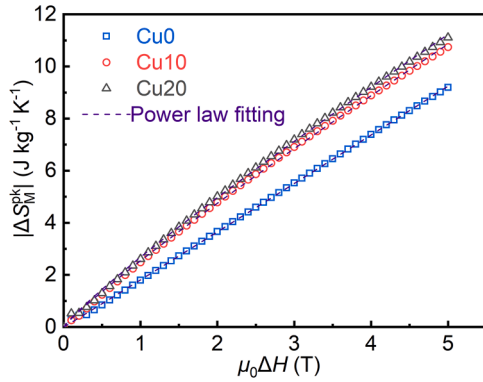


Fig. 11. The  $\mu_0\Delta H$  dependence of  $|\Delta S_M^{\text{pk}}|$  for Cu0, Cu10 and Cu20 alloys. The dashed lines are fitting curves.

Table 3

The exponent  $b$  and the determination coefficients of the fitting,  $R^2$ , for the Cu0, Cu10 and Cu20 alloys.

Sample	Cu0	Cu10	Cu20
$b$	1.01251	0.90155	0.88939
$R^2$	0.99987	0.99958	0.99948

= 40.74 K, 45.52 K, 43.22 K for Cu0, Cu10 and Cu20 alloys, respectively. According to the principles of statistical theory, the critical exponents  $\beta$ ,  $\gamma$  and  $\delta$  must satisfy the Widom scaling relation [91]:

$$\delta = 1 + \gamma/\beta \quad (12)$$

Therefore, the critical exponent  $\delta$  is calculated as  $\delta = 3.228 \pm 0.025$ ,  $3.250 \pm 0.005$ ,  $3.422 \pm 0.003$  for Cu0, Cu10 and Cu20 alloys,

respectively. Furthermore, the critical exponents  $\beta$ ,  $\gamma$  and  $\delta$  can also be determined using the Kouvel-Fisher (KF) method by reformulating Eqs. (8) and (9) in an alternative direction [92]:

$$M_s(T)[dM_s(T)/dT]^{-1} = (T - T_c)/\beta \quad (13)$$

$$\chi_0^{-1}(T)[d\chi_0^{-1}(T)/dT]^{-1} = (T - T_c)/\gamma \quad (14)$$

In this method,  $M_s(T)[dM_s(T)/dT]^{-1}$  vs.  $T$  and  $\chi_0^{-1}(T)[d\chi_0^{-1}(T)/dT]^{-1}$  vs.  $T$  are plotted for all alloys on the same figures, yielding straight lines with slopes of  $1/\beta$ ,  $1/\gamma$ , respectively, and intersecting the temperature axis at  $T_c$ . The exponents derived from the linear fitting are utilized to generate a revised Arrott-Noakes plot. Fig. 12d-f shows the results of  $M_s(T)[dM_s(T)/dT]^{-1}-T$  and  $\chi_0^{-1}(T)[d\chi_0^{-1}(T)/dT]^{-1}-T$  and their linear fitting curves for all alloys. For temperatures below  $T_c$ , the critical exponent  $\beta$  is determined as  $\beta_{\text{KF}} = 0.643 \pm 0.004$ ,  $0.611 \pm 0.007$ ,  $0.562$

$\pm 0.005$  with the Curie temperatures being  $T_{c1} = 39.30 \pm 0.25$  K,  $45.35 \pm 0.35$  K,  $43.27 \pm 0.25$  K for the Cu0, Cu10 and Cu20 alloys, respectively. For temperatures above  $T_c$ , the critical exponent  $\gamma$  is determined as  $\gamma_{\text{KF}} = 1.415 \pm 0.009$ ,  $1.374 \pm 0.005$ ,  $1.373 \pm 0.010$ , with the Curie temperatures identified as  $T_{c2} = 41.20 \pm 0.37$  K,  $45.80$

$\pm 0.30$  K,  $43.22 \pm 0.20$  K for the Cu0, Cu10 and Cu20 alloys, respectively. The critical exponent  $\delta$ , as defined by Eq. (12), is determined to be  $\delta_{\text{KF}} = 3.201 \pm 0.026$ ,  $3.249 \pm 0.022$ ,  $3.443 \pm 0.015$  for the Cu0, Cu10 and Cu20 alloys, respectively. The critical exponents for all alloys, obtained using the MAP and KF methods, are presented in Table 4 for comparison. The consistency between the results derived from the two methods validates the accuracy and reliability of the obtained critical exponents. The exponent  $\beta$  is significantly higher than the theoretical value of the 3D Heisenberg model (0.365) and even exceeds that of the mean field model (0.5). However, the exponent  $\gamma$  closely matches the



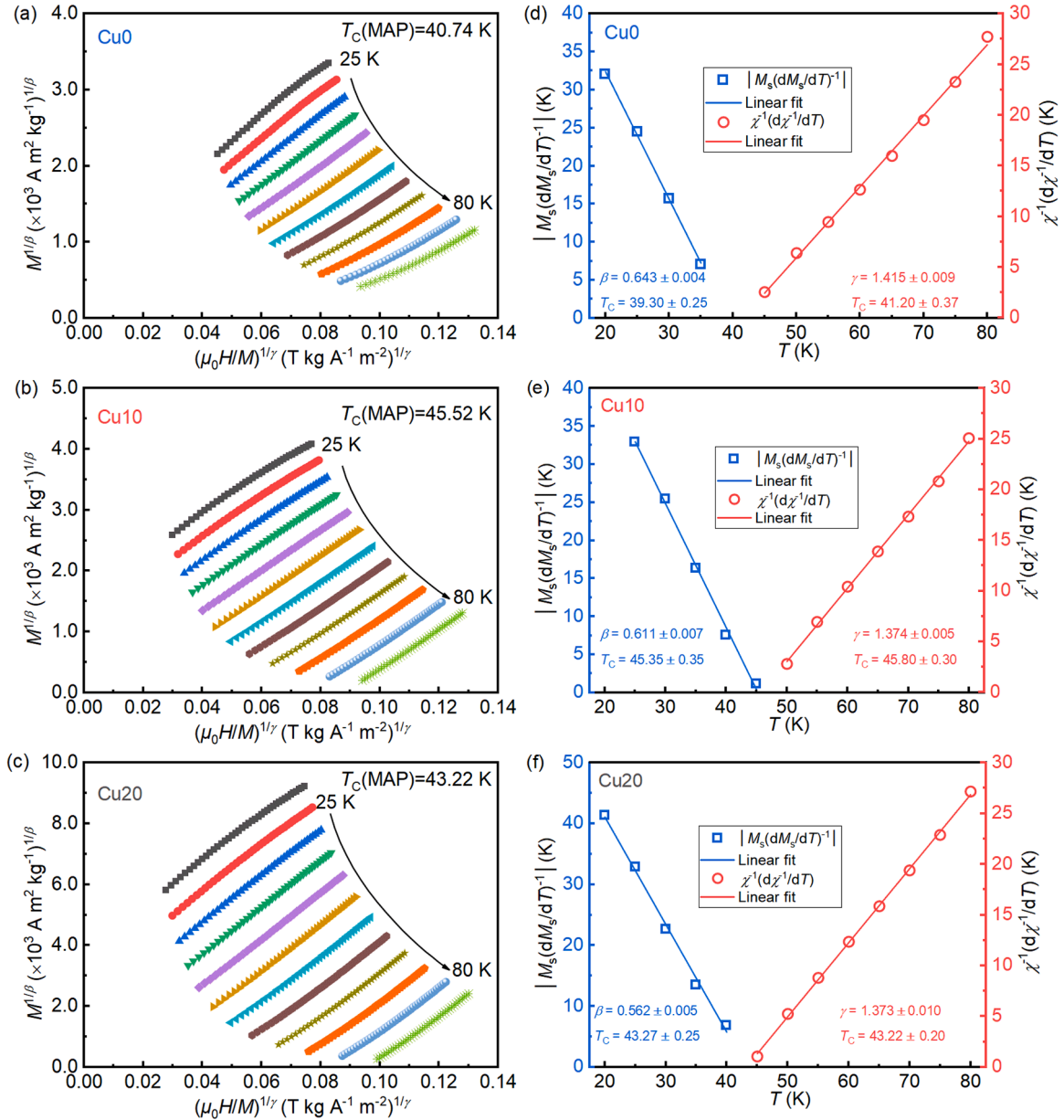


Fig. 12. (a)-(c) MAP plots of the Cu0, Cu10 and Cu20 alloys, respectively; (d)-(f) KF plots for the Cu0, Cu10 and Cu20 alloys, respectively.

theoretical value of the 3D Heisenberg model (1.336). This situation is similar to that of the reported  $\text{Gd}_{60}\text{Fe}_{20}\text{Al}_{20}$  microwires [47], where the  $\beta$  value is relatively large, and the  $\gamma$  value is close to the theoretical value of the 3D Ising model. It is noteworthy that the  $\gamma$  values of Cu10 and Cu20 are similar, while the  $\gamma$  value of Cu0 is relatively higher. It is widely recognized that  $\beta$  characterizes the growth of the ordered moment below  $T_C$ , whereas  $\gamma$  describes the divergence of the magnetic susceptibility at  $T_C$ . A smaller  $\beta$  value indicates a more rapid growth in the ordered moment [47]. In this study, the studied alloys exhibit coexisting FM interactions between RE-RE (Gd, Ho, Er) and AFM interactions between Ni-RE (Gd, Ho, Er). The long-range behavior of FM interactions is disrupted by the AFM interactions, which break the long-range order and induce short-range ordering below  $T_C$ . Furthermore, the short-range AFM interaction exists in the nanometer-scale amorphous phase of the Cu0 alloy. These factors may result in relatively high critical exponent  $\beta$  values for the studied alloys, with Cu0 exhibiting the highest value. Moreover, the variation trends of  $n$  around  $T_C$  and exponent  $b$  are consistent with the  $\gamma$  values, indicating the effectiveness of  $n$  and  $b$  in analyzing the critical behavior near the phase

transition.

Table 2 shows the magnetocaloric parameters for the studied alloys and other reported RE-containing HE-MGs working in the temperature range of 20–77 K. To visually compare the MCE properties of these alloys, the  $T_C$  dependence of  $|\Delta S_M^{\text{pk}}|$  for these alloys were plotted in Fig. 13. It can be observed from this image that the Cu10 and Cu20 alloys exhibit the relatively high  $|\Delta S_M^{\text{pk}}|$ . The comparable MCE properties and SOMET lead to a significant potential application of Cu10 and Cu20 alloys as high-performance magnetic refrigerants within temperature range required by hydrogen liquefaction (20–77 K).

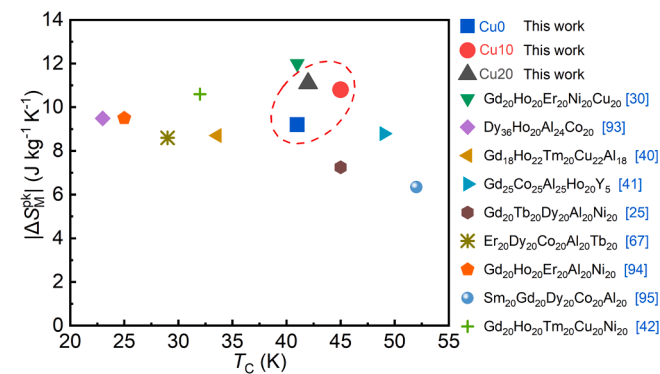
#### 4. Conclusions

The designed Cu0, Cu10 and Cu20 alloys were prepared through melt-spinning technology. The structure of these alloys evolves from an amorphous/nanocrystalline dual-phase structure in the Cu0 alloy to a fully amorphous structure in the Cu10 and Cu20 alloys. The enhanced GFA induced by Cu addition leads to the fully amorphous structures of

**Table 4**

The  $T_C$  and critical exponents of the Cu0, Cu10 and Cu20 alloys in comparison with those of the theoretical models.

Material/Model	Method	$T_C$ (K)	$\beta$	$\gamma$	$\delta$	Refs.
Mean field	Theory	-	0.5	1.0	3.0	[89]
3D Heisenberg	Theory	-	0.365	1.336	4.80	[89]
3D Ising	Theory	-	0.325	1.241	4.82	[89]
Tricritical mean field	Theory	-	0.25	1.0	5.0	[90]
Cu0	MAP	40.74	0.641	1.428	3.228	This work
	KF (below $T_C$ )	39.30	0.643	-	3.201	
	KF (above $T_C$ )	41.20	-	1.415	-	
Cu10	MAP	45.52	0.614	1.381	3.250	This work
	KF (below $T_C$ )	45.35	0.611	-	3.249	
	KF (above $T_C$ )	45.80	-	1.374	-	
Cu20	MAP	43.22	0.566	1.370	3.422	This work
	KF (below $T_C$ )	43.27	0.562	-	3.443	
	KF (above $T_C$ )	43.22	-	1.373	-	



**Fig. 13.** The  $T_C$  dependence of  $|\Delta S_M^{pk}|$  for the studied alloys and other reported RE-containing HE-MGs at  $\mu_0 H = 5$  T.

Cu10 and Cu 20 alloys. All studied alloys exhibit SOMT. The  $T_C$  values for the Cu0, Cu10 and Cu20 alloys are close, i.e., 41, 45, and 42 K, respectively. All studied alloys possess uniform elemental distribution, except for the Ni enrichment in the minor amorphous phase of the Cu0 alloy, leading to a significant compositional difference between nanocrystalline phase of the Cu0 alloy and the amorphous phases of the Cu10 and Cu20 alloys. This, combined with the structural difference between the Cu-free alloy and Cu-added alloys, leads to the relatively higher  $|\Delta S_M^{pk}|$  values of the Cu10 and Cu20 alloys (10.8 and 11.1 J kg<sup>-1</sup> K<sup>-1</sup>, respectively) compared to the Cu0 alloy (9.2 J kg<sup>-1</sup> K<sup>-1</sup>) at  $\mu_0 H = 5$  T, as well as notable differences in critical exponents near phase transitions between the Cu-free and Cu-added alloys. In addition, the coexistence of AFM and FM interactions results in relatively large critical exponent  $\beta$  values for all the studied alloys, with Cu0 exhibiting the highest value. The Cu10 and Cu20 alloys possess the comparable MCE properties with respect to those of the reported RE-containing HE-MGs with the similar  $T_C$ , making them suitable as the high-performance magnetic refrigerants within temperature range required by hydrogen liquefaction (20–77 K).

#### CRediT authorship contribution statement

**Chen Fan:** Investigation, Formal analysis. **Ma Yunshuang:**

Investigation, Formal analysis. **Gao Meng:** Project administration, Investigation, Funding acquisition. **Song Lijian:** Supervision, Project administration, Methodology, Investigation, Funding acquisition, Formal analysis. **Zhang Yan:** Supervision, Funding acquisition, Formal analysis. **Xu Wei:** Supervision, Formal analysis. **Wang Jun-Qiang:** Writing – review & editing, Supervision, Project administration, Methodology, Investigation, Funding acquisition. **Huo Juntao:** Writing – review & editing, Supervision, Project administration, Methodology, Investigation, Funding acquisition, Formal analysis. **Pei Zhongwei:** Writing – original draft, Investigation, Formal analysis. **Yin Hangbo:** Writing – review & editing, Supervision, Project administration, Methodology, Investigation, Funding acquisition, Formal analysis, Data curation.

#### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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#### Data availability

Data will be made available on request.

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